

$$\sum \tau = 0 \quad A \cdot 2l - F \cdot l = 0 \rightarrow \boxed{A = \frac{F}{2}}$$

$$M(x_1) = -A \cdot x_1$$

$$EI_y \cdot w''(x_1) = A \cdot x_1$$

$$EI_y \cdot w'(x_1) = A \cdot \frac{x_1^2}{2} + C_1$$

$$EI_y \cdot w(x_1) = A \cdot \frac{x_1^3}{6} + C_1 x_1 + C_2$$

$$w(0) = 0 \rightarrow \underline{C_2 = 0}$$

$$w(2l) = 0 \rightarrow A \cdot \frac{8l^3}{6} + C_1 \cdot 2l = 0$$

$$\frac{F}{2} \cdot \frac{4}{3} l^3 + C_1 \cdot 2l = 0$$

$$\underline{C_1 = -\frac{1}{3} F l^2}$$

$$M(x_2) = -F \cdot x_2$$

$$EI_y \cdot w''(x_2) = F \cdot x_2$$

$$EI_y \cdot w'(x_2) = F \cdot \frac{x_2^2}{2} + C_3$$

$$EI_y \cdot w(x_2) = \frac{F x_2^3}{6} + C_3 x_2 + C_4$$

$$w'(l) = 0$$

$$\varphi_1(2l) = -\varphi_2(l)$$

$$\frac{F \cdot 4l^2}{4} - \frac{1}{3} F l^2 = -\frac{F l^2}{2} - C_3$$

$$F l^2 - \frac{1}{3} F l^2 + \frac{F l^2}{2} = C_3 \rightarrow \underline{\underline{C_3 = -\frac{7}{6} F l^2}}$$

$$w(l) = 0$$

$$0 = \frac{F l^3}{6} - \frac{7}{6} F l^3 + C_4$$

$$\underline{C_4 = F l^3}$$

$$w(0) = \frac{1}{EI_y} \left(\frac{F \cdot 0}{6} - \frac{7}{6} F l^2 \cdot 0 + F l^3 \right)$$

$$\boxed{w(0) = \frac{F l^3}{EI_y}}$$



$$I \quad \curvearrowright \quad B_F \cdot 2l - \frac{1}{2} l \cdot F \cdot \left(\frac{4l}{3}\right) = 0$$

$$\underline{B_F = \frac{2}{3} F l^2}$$

$$II. \quad \curvearrowright \quad M_{CF} - B_F \cdot l - \frac{1}{2} l \cdot F \cdot \frac{2}{3} l = 0$$

$$M_{CF} = \frac{2}{3} F l^3 + \frac{1}{3} F l^3 = F l^3$$

$$M_B(x_2) = -M_{CF} + \frac{1}{2} x_2 \cdot F \cdot x_2 + \frac{2}{3} x_2^2 \cdot x_2 = \frac{M_{FD}(x_2)}{l} = \frac{F l}{l}$$

$$M_{FD}(x_2) = F \cdot x_2$$

$$w(x_2) = \frac{M_B(x_2)}{EI_y} = \frac{-M_{CF}}{EI_y} = \frac{-F l^3}{EI_y}$$

$$\underline{v_2 = 0}$$



$$A = \frac{Fl}{2}$$

$$F \rightarrow \frac{1}{2} F \cdot w = W$$

$$\frac{1}{3} + \frac{1}{6} = \frac{2}{6} + \frac{1}{6} = \frac{3}{6}$$

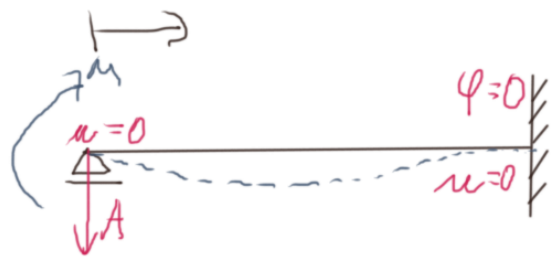
$$U = \int \frac{M(x)^2}{2EI_y} = \int_0^{2l} \frac{F^2 \cdot x_1^2}{4 \cdot 2EI_y} dx_1 + \int_0^l \frac{F^2 \cdot x_2^2}{2EI_y} dx_2 =$$

$$\frac{1}{2}$$

$$= \frac{F^2}{8EI_y} \left[\frac{x_1^3}{3} \right]_0^{2l} + \frac{F^2}{2EI_y} \left[\frac{x_2^3}{3} \right]_0^l = \frac{F^2 \cdot 8l^3}{8 \cdot EI_y \cdot 3} + \frac{F^2 l^3}{6EI_y}$$

$$\frac{1}{2} \frac{F l^3}{EI_y} = \frac{1}{2} F \cdot w$$

$$w = \frac{Fl^3}{EI_y}$$



BDR

$$M(x) = M - A \cdot x$$

$$EI_y w''(x) = A \cdot x - M$$

$$EI_y w'(x) = A \frac{x^2}{2} - M \cdot x + C_1$$

$$EI_y w(x) = A \frac{x^3}{6} - M \frac{x^2}{2} + C_1 x + C_2 \stackrel{=0}{}$$

$$w(0) = 0 \rightarrow \underline{\underline{C_2 = 0}}$$

$$\varphi(l) = 0 ; \left[\begin{aligned} A \frac{l^2}{2} - Ml + C_1 &= 0 \\ C_1 &= Ml - A \frac{l^2}{2} \end{aligned} \right]$$

$$w(l) = 0$$

$$0 = A \frac{l^3}{6} - M \frac{l^2}{2} + C_1 \cdot l$$

$$0 = A \frac{l^3}{6} - M \frac{l^2}{2} + Ml^2 - A \frac{l^3}{2}$$

$$0 = \frac{Ml^2}{2} - \frac{1}{3} Al^3$$

$$\boxed{A = \frac{3M}{2l}}$$

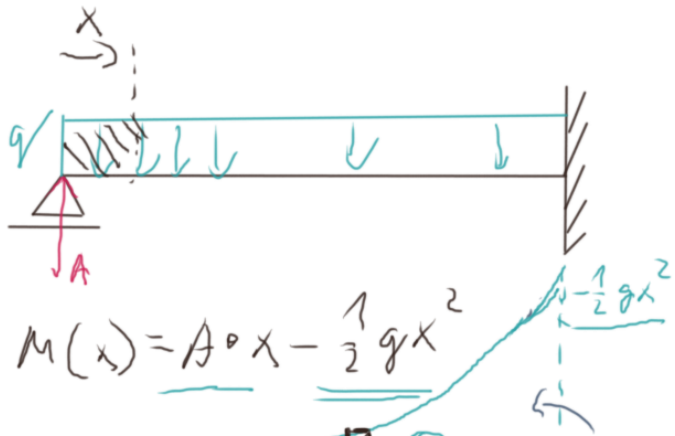


$$M = A \cdot x + M$$



$$M \cdot l - \frac{A \cdot l \cdot l}{3} = 0$$

$$A = \frac{3M}{2l}$$



FN

$x_T = \frac{\int x dA}{\int dA} = \frac{\int x \cdot \frac{1}{2} q x^2 dx}{\int \frac{1}{2} q x^2 dx} \Rightarrow$

$dA = \frac{1}{2} q x^2 \cdot dx$

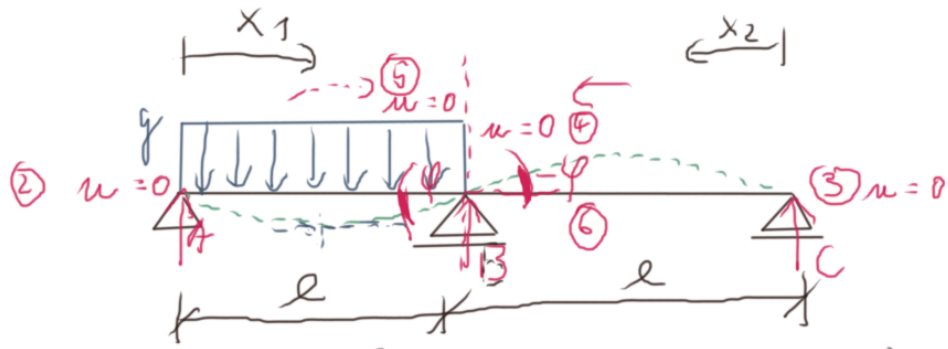
$\circlearrowleft 0 = \frac{1}{EI} \left(\frac{q l^3}{24} \cdot \frac{3}{4} l - \frac{A l^2}{2} \cdot \frac{2}{3} l \right)$

$\frac{q \cdot l^4}{8} = \frac{A \cdot l^3}{3}$

$A = \frac{3}{8} q l$

$\frac{q}{2} \left[\frac{x^4}{4} \right]_0^l = \frac{3}{4} l$

$\frac{q}{2} \left[\frac{x^3}{3} \right]_0^l = \frac{3}{4} l$



$$A \cdot l - q \cdot l \cdot \frac{l}{2} - C \cdot l = 0$$

$$\textcircled{1} \quad A - \frac{q \cdot l}{2} = C$$

Wahlmomen: A, C, C_1, C_2, C_3, C_4

$$M(x_1) = A \cdot x_1 - \frac{1}{2} q x_1^2$$

$$EI_y w''(x_1) = \frac{1}{2} q x_1^2 - A \cdot x_1$$

$$EI_y w'(x_1) = \frac{1}{6} q x_1^3 - A \frac{x_1^2}{2} + C_1$$

$$EI_y w(x_1) = \frac{1}{24} q x_1^4 - A \cdot \frac{x_1^3}{6} + C_1 x_1 + C_2$$

$$\textcircled{2} \quad w(0) = 0 \rightarrow C_2 = 0$$

$$\textcircled{5} \quad w(l) = 0 \rightarrow C_1 = \frac{A l^2}{6} - \frac{1}{24} q l^3$$

$$M(x_2) = C \cdot x_2$$

$$EI_y w''(x_2) = -C x_2$$

$$EI_y w'(x_2) = -C \frac{x_2^2}{2} + C_3$$

$$EI_y w(x_2) = -C \frac{x_2^3}{6} + C_3 x_2 + C_4$$

$$\textcircled{3} \quad w(0) = 0 \rightarrow C_4 = 0$$

$$\textcircled{4} \quad w(l) = 0 \rightarrow -C \frac{l^3}{6} + C_3 \cdot l = 0 \rightarrow C_3 = \frac{1}{6} C \cdot l^2$$